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Looking for sp^2 Carbon Atoms in Diamond: a Quantum Mechanical Study of Interacting Vacancies.

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This paper reports the calculated relaxed lattice configurations and corresponding electronic and magnetic structures, and Raman frequencies of two divacancies in diamond, V_2 and $VC=CV$, in which the vacancies are first and third neighbours respectively. The calculations are formulated within a supercell approach to local defects in crystalline solids, here 64- and 128-atoms unit cells and based largely on the B3LYP one-electron approximation constructed from an all-electron Gaussian basis set. Three important findings are first, that, of the four possible spin states, $S_z=0, 1, 2, 3$, the singlet is predicted to be lowest in energy for both divacancies; second, that the singlet state of V_2 is ~ 1.7 eV lower in energy than that in $VC=CV$; and third, that the Raman peak at 1628 cm^{-1} in defective diamond can be ascribed to the presence of a $C=C$ double bond, as in the singlet state of $VC=CV$.

I. INTRODUCTION

There has been long-standing theoretical^{1–5} and experimental^{6–9} interest in both native and radiation-induced defects in semiconductors. Of these, diamond, with a wide band gap, high Young’s modulus, thermal conductivity and carrier mobility, and broad transparency range, has found widespread application in areas as diverse as micromechanical systems, heat sinks, laser windows and particle detectors.^{10,11} However, it is known that the presence of defects can have a dramatic effect on its structural¹², optical¹³ and electronic¹⁴ properties. Clearly, then, both from a technological point of view, and diamond science more generally, an accurate, quantitative understanding of defects, which to some extent are always present, is important, not least in the interpretation of the plethora of often confusing and contradictory experimental data.^{15–20} Of many experimental techniques that might be used to study diamond, and the more stable allotrope, graphite, vibrational spectroscopy, both infra-red and Raman, has been found to be particularly useful, for the different bonding in these systems, viz., sp^3 and sp^2 respectively, leads to characteristic vibrational frequencies, so that the presence of sp^2 electrons associated with vacancies in diamond, for example, might be detectable in this way. Consequently, vibrational spectroscopy has emerged as an important, further technique in the investigation of defect formation in irradiated diamond.^{15,16,20–28}

The Raman spectrum of pristine diamond consists of a single, sharp peak at 1332 cm^{-1} corresponding to the first-order scattering of triply-degenerate $TO(X)$ phonons of t_{2g} symmetry.²⁹ The irradiation-damaged crystal, on the other hand, exhibits several additional features which have been attributed to a variety of defects containing sp^2 and sp^3 electronic configurations. The most prominent of these to higher frequency than the first order line are located at about 1450 , 1490 , 1630 and 1680

cm^{-1} . The latter two have commonly been attributed to defects such as the “dumb-bell” split-interstitial containing sp^2 electrons^{15,23}, while the peaks at 1450 and 1490 cm^{-1} have variously been attributed to both vacancy and carbon/nitrogen interstitial defects.^{30,31} Moreover, the first-order Raman peak is both broadened and red-shifted in damaged crystals.^{23,27,30,31} This can tentatively be explained by noting that the peak frequency in pristine material depends primarily on the C-C bond length (and strength), and that if the former is increased in the damaged crystal, this would lead to a red-shift, *i.e.* lowering, of the original Raman frequency. As a result of recent theoretical developments³² and computational implementation of fully-analytic quantum mechanical methods for the *ab initio* evaluation of infra-red and Raman spectra in solids^{32–35}, computational vibrational spectroscopy is now established as an additional and effective tool in the interpretation of experimental spectra.^{36–38} Accordingly, as a first step towards a more complete quantitative understanding of defective diamond, this paper reports the computed Raman spectra of the two lowest spin states of two neutral divacancies, V_2 and $VC=CV$, in which the vacancies are first and third neighbours (as reported in Figure 1), each at concentrations of $(1/64)$ and $(1/128)$ defects per carbon. These are compared to previous experimental and theoretical data.³⁹

II. COMPUTATIONAL DETAILS

The calculations reported here are of two types: the first involves the quantum mechanical determination of the optimum, *i.e.* energy-minimised, lattice structure (atomic positions), total energy and electronic and spin structures of both perfect and defective diamond lattices based on periodic supercells; the second is the calculation of the phonon spectra, and from these the Raman active frequencies and intensities of the previously cal-

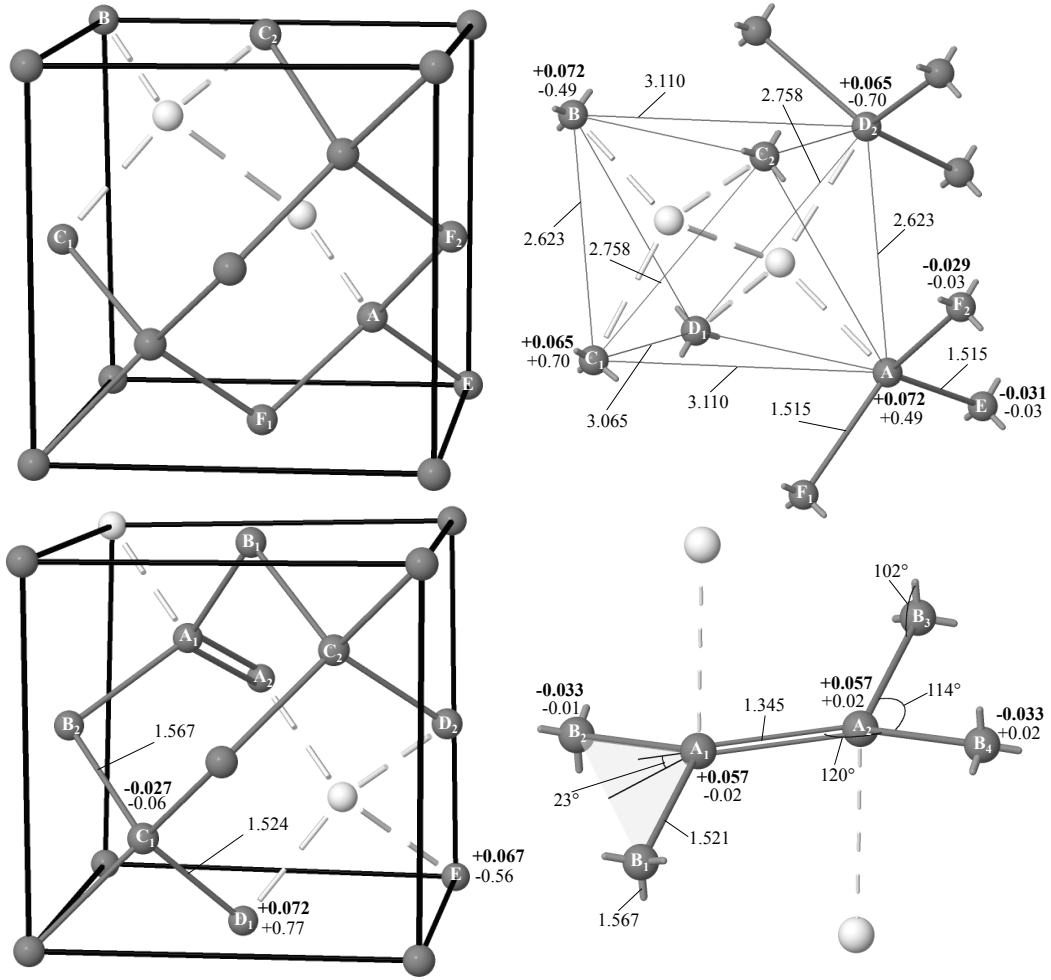


FIG. 1: B3LYP equilibrium geometries, net Mulliken charges and spin moments for the divacancies, V₂ (upper right) and VC=CV (lower right) based on S₆₄, where interatomic distances (normal) are in Å and angles in degrees. The equivalent conventional diamond cells are shown on the left, where atomic Mulliken net charges (bold) and spin moments (normal) are in $|e|$. White spheres represent vacancies, and dashed white lines their nearest neighbour connectivity.

culated structures and energy/displacement derivatives using recently implemented methods for calculating the infra-red and Raman spectra of solids.^{32–35} In order to simulate the presence of vacancies in both defective structures, a complete removal of the atoms of interest (nuclei, electrons, basis set) has been performed. The majority of electronic structures and energies were obtained from the well-established B3LYP^{40,41} hybrid implementation of density functional theory (DFT) in both spin un-polarised and unrestricted spin polarised descriptions using the CRYSTAL code.³² The B3LYP approximation has been shown to give vibrational properties of solids that are comparable to, and in some cases superior to, those from other functionals.^{37,38,42} An important feature of both the vacancies examined here is that they contain six unbound sp^3 electrons, which can give rise to four spin states, $\{\alpha\alpha\alpha\beta\beta\beta\}_{S_z=0}$, $\{\alpha\alpha\alpha\alpha\beta\beta\}_{S_z=1}$, $\{\alpha\alpha\alpha\alpha\alpha\beta\}_{S_z=2}$ and $\{\alpha\alpha\alpha\alpha\alpha\alpha\}_{S_z=3}$, for which we have used spin unre-

stricted hybrid DFT. Previous calculations for a diversity of open-shell systems^{43–47} have shown that despite the evident deficiency with respect to S^2 , but not S_z , this approach leads to acceptable, often accurate, descriptions of the magnetism. The use of 64- and 128-unit supercells, S₆₄ and S₁₂₈, serves the twin purposes of investigating whether the vacancies are essentially isolated at these defect concentrations, and if not, the extent of the interaction. Crucial to the reliable prediction of formation energies and Raman frequencies, is the accurate calculation of the equilibrium structures of the defective crystal. To achieve this, the lattice parameters and *all* atomic positions of both the S₆₄ and S₁₂₈ unit cells have been optimised to a root mean square (r.m.s.) displacement of 10^{-5} Å. For the limited purposes of checking the formation energies of the two divacancies, PBE0⁴⁸ and HSE06⁴⁹ hybrid functionals have also been explored, in addition to the unscreened HF approximation and the

inclusion of Grimme’s empirical dispersion correction⁵⁰ to the B3LYP potential.

In keeping with the use of the B3LYP, PBE0 and HSE06 functionals in their “standard” form, *i.e.* without any empirical adjustments in respect of the calculated Raman frequencies, Pople’s (standard) 6-21G Gaussian basis set⁵¹ has been adopted for the Bloch function expansions, except for the exponent of the most diffuse *sp* shell, which has been re-optimised (0.228 Bohr^{-2}) to minimise the energy of non-defective bulk diamond. Again, to check the divacancy formation energies, B3LYP calculations have also been carried out using 6-21G*, 6-31G and 6-31G* basis sets⁵²; and for comparisons with previous reports, the PBE gradient corrected⁵³ and uncorrected LDA functionals⁵⁴ have also been examined. The computational parameters used in this report comprise five values (T_1 – T_5) that control the truncation of the (infinite) Coulomb and exchange series³², here set to 10^{-8} (T_1 – T_4) and 10^{-16} (T_5); the SCF energy convergence threshold, which in this study was set to 10^{-8} Ha for structural optimisation and 10^{-10} Ha for the vibration frequency calculations; and the shrinking factors that control the number of independent **k**-points used in the sampling of the Monkhorst-Pack⁵⁵ net, here 150 and 24 points for S_{64} and S_{128} respectively.

For the lattice dynamics calculations, harmonic phonon frequencies, ω_p , were evaluated at the Γ point and obtained from the diagonalization of the mass-weighted Hessian matrix (second energy derivatives with respect to atomic displacements $u^{36,56,57}$)

$$W_{ai,bj}^\Gamma = \frac{H_{ai,bj}^0}{\sqrt{M_a M_b}} \quad \text{with} \quad H_{ai,bj}^0 = \left(\frac{\partial^2 E}{\partial u_{ai}^0 \partial u_{bj}^0} \right), \quad (1)$$

where atoms a and b (with atomic masses M_a and M_b) in the reference cell, **0**, are displaced along the i -th and j -th Cartesian directions, respectively. First order derivatives were computed analytically, whereas second order derivatives were obtained numerically, using a two-point formula. The Raman intensity, $I_{ii'}^p$, corresponding to the Stokes’ line of a phonon mode Q_p , can be expressed as

$$I_{ii'}^p \propto \left(\frac{\partial \alpha_{ii'}}{\partial Q_p} \right)^2, \quad (2)$$

where $\alpha_{ii'}$ is the ii'^{th} component of the polarizability tensor α . Here the relative values of these intensities were computed analytically using a procedure recently implemented in the CRYSTAL code.^{34,35}

III. RESULTS

A. Equilibrium structure, relative energies and electronic structure

Except where explicitly cited, the results reported in this section refer to B3LYP calculations, and energies, to

TABLE I: B3LYP relative stability, ΔE , and formation energy, E_f , for different spin states of V_2 and $VC=CV$ based on S_{64} and S_{128} . Also given are $2 \times E_f$ for the isolated vacancy.

	S_z	ΔE_{64}	E_{64}^f	ΔE_{128}	E_{128}^f
$VC=CV$	0	-	11.67	-	11.70
	1	0.068	11.74	0.084	11.78
	3	1.741	13.41	1.758	13.46
V_2	0	-	9.94	-	9.96
	1	0.060	9.99	0.057	10.01
	3	2.152	12.09	2.144	12.10
V_1	0	-	13.50	-	13.50
	1	0.217	13.94	0.223	13.94
	2	1.423	16.34	1.426	16.34

the optimised (equilibrium) structures. Despite the evident differences between the local lattice structures surrounding V_2 and $VC=CV$, the spin configurations of the lowest energy states were found to be identical, which greatly facilitates comparisons between the two. Preliminary calculations ruled out $S_z=2$ on energy grounds, leaving the singlet, triplet and septet states for detailed examination. In the singlet state, the spins align $\{\alpha\alpha\beta\}$ on the three surrounding atoms of one vacancy, and $\{\alpha\beta\beta\}$ around the other; whereas in the triplet state, the spin alignment is either $\{\alpha\alpha\beta\}$ or $\{\alpha\beta\beta\}$ around *both* vacancies. There is just one septet alignment. The relative stability, ΔE , of the three lowest energy spin states of V_2 and $VC=CV$ based on S_{64} and S_{128} are listed in Table I. The singlet state is found to be the most stable for both divacancies, with the triplet state slightly less stable, by (2.1 - 2.2) meV and (2.5 - 3.1) meV respectively for V_2 and $VC=CV$. The septet state is a further (60-80) meV higher in energy. For the isolated vacancy, the singlet-triplet difference⁴⁴ is approximately twice the divacancy values. Hyde-Volpe *et al.*³⁹ have reported a similar order of stability based on BLYP cluster calculations, with a difference of ~ 8 meV between the singlet and triplet for the two divacancies, which is roughly three times that obtained here.

The formation energy of a defect is commonly given by,

$$E_f = E_P - E_D - nE_A \quad (3)$$

where E_P and E_D are the total energies of the pristine and defective diamond supercells, respectively, E_A is the energy *per atom* in bulk diamond and n is the number of vacancies in the unit cell, here 2. For comparison, the energies of the isolated vacancy are doubled. The values of E_f given in Table I show quite clearly that V_2 is more stable than $VC=CV$ for all three spin states, with differences in energy varying from ~ 1.7 eV for the singlet and triplet states to ~ 1.3 eV for the septet. Table I also indicates that the association, or binding energy of two (isolated) $S_z=0$ vacancies to form a singlet V_2 is ~ 3.5 eV.

To examine the effects of basis sets of higher quality than Pople’s 6-21G, the formation energies, E_f , of singlet V_2

and VC=CV were calculated using 6-21G, 6-21G^{opt}, 6-21G*, 6-31 and 6-31* basis sets, where 6-21G^{opt} contains the optimised outer *sp* exponent. These are given in Table II which shows that for the singlet state of both V₂ and VC=CV the maximum deviation from the 6-21G^{opt} value of E_f is 1.6%, while the average difference in E_f between the two divacancy values for the richer bases, 1.7 eV, is identical to the 6-21G^{opt} value. Changes in hybrid functional have also been examined. Table III contains singlet formation energies of V₂ and VC=CV based on LDA, UHF and four other hybrid approximations based on S_{64} . Also included are values reported by Hyde-Volpe *et al.*³⁹ based on both cluster and periodic supercell calculations. Once again, of prime concern is the variation in the formation energies of singlet V₂ and VC=CV with changes in exchange-correlation functional, and the differences between the two divacancies. As observed, UHF estimates for E_f deviate most from the B3LYP values, with decreases of 12% and 8% for V₂ and VC=CV respectively, although the difference between the two formation energies, 1.9 eV, remains much the same (1.7 eV). For both vacancies, the average of the alternative functional values for E_f , 9.86 eV and 11.79 eV, differ by <1% from the B3LYP energies, while the average relative stability of V₂ is increased by 0.2 eV (11%). The local geometries (atomic positions), net Mulliken

TABLE II: Formation energy (E_f) for V₂ and VC=CV from 6-21G, 6-21G^{opt}, 6-21G*, 6-31 and 6-31* basis sets. Energy differences (δE_f) with respect to 6-21G^{opt} are reported as well. $\Delta E_f = E_f(\text{VC=CV}) - E_f(\text{V}_2)$.

Basis set	V ₂		VC=CV		ΔE_f
	E_f	δE_f	E_f	δE_f	
6-21G	9.88	0.06	11.76	-0.09	1.88
6-21G ^{opt}	9.94	–	11.67	–	1.73
6-21G*	9.78	0.16	11.48	0.19	1.70
6-31	9.84	0.10	11.56	0.11	1.72
6-31*	9.78	0.16	11.52	0.15	1.74

TABLE III: Formation energy E_f^f (in eV) for the $S_z = 0$ spin state of the VC=CV, V₂ defects in diamond obtained with HF, various DFT functionals and the S_{64} . ^{a)} Cluster calculation with the open shell singlet configuration, C_{190-n}H₁₁₀. ^{b)} Periodic boundary condition supercell calculation with the open shell singlet configuration.

	Method	$E_{\text{VC=CV}}^f$	$E_{\text{V}_2}^f$	$2 \times E_{\text{V}_1}^f$ ⁴⁴
This work	UHF	10.73	8.82	11.92
	B3LYP	11.67	9.94	13.46
	B3LYP+D3	11.83	10.10	14.14
	PBE0	12.47	10.53	14.20
	HSE06	12.37	10.44	13.98
	PBE	11.29	9.40	13.04
	LDA	11.92	9.89	14.02
Ref. 39	BLYP ^a	12.56	10.37	15.24
	PBE ^b	9.21	7.81	12.14

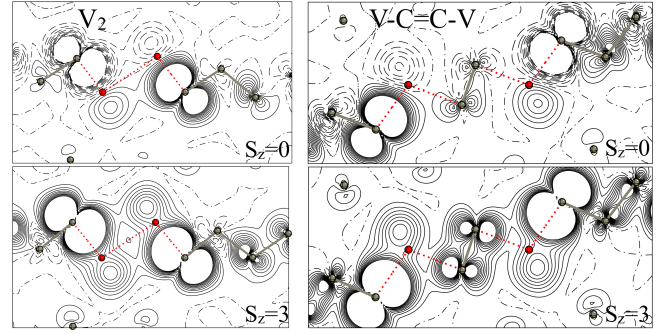


FIG. 2: B3LYP spin density maps of the V₂ and VC=CV defect in diamond for $S_z=0$ (upper panel) and $S_z=3$ (lower panel) spin states. Red circles represent the two vacancies while dotted red lines connect the vacancy to its nearest neighbours. Isodensity lines differ by 0.01 $|e|/(a_0)^3$; spin density is truncated at $\pm 0.1 |e|/(a_0)^3$. Continuous, dashed and dot-dashed black lines indicate positive, negative and zero values, respectively.

charges and spin moments of the V₂ and VC=CV defects are shown in Figure 1, where the numerical values refer to the singlet, $S_z=0$, spin state for the S_{128} cell.

As shown in the lowest part of Figure 1, there is a substantial re-arrangement of the six central atoms of the VC=CV divacancy to give a structure which is not too dissimilar to that of the tetramethyl ethylene molecule, TME (CH₃)₂C=C(CH₃)₂. Thus, the out-of-plane angle, defined therein as the angle between the A₁, B₁ and B₂ plane and the double bond axis, A₁-A₂, is 23°, while the angles B₂Ā₁B₁ and B₃Ā₂B₄ are 114° and A₁Ā₂B₄ and A₂Ā₁B₁ 120°. Mulliken analyses indicate strong spin localisation at the three atoms nearest neighbours to each vacancy, the most stable of many possible spin distributions leading to local moments of (+0.77 $|e|$, +0.77 $|e|$, -0.56 $|e|$) around one vacancy and moments of the opposite sign around the other, so that the total S_z is zero. The A₁-A₂ and A₁-B₁ (and equivalent) distances of 1.345 Å and 1.521 Å, respectively, are close to electron diffraction values of 1.351 Å and 1.516 Å reported for TME⁵⁸, while the double bond distance is also close to that of 1.325 Å, which is calculated for (molecular) ethylene using an identical basis set and functional, whereas the next C-C distances away from the defect essentially coincide with the perfect bulk value of 1.560 Å. The local geometries of the other spin states are close to that of the singlet. On the other hand, as the upper part of Figure 1 shows, in the case of the V₂ divacancy, it is only the local (nn) lattice surrounding the defect that is appreciably perturbed, for the bond distances and tetrahedral angles second neighbour to the vacancies are extremely close to the pure diamond values. For the singlet state, Mulliken analyses indicate again a strong spin localisation at the three atoms nearest neighbours to each vacancy, leading to local moments of (+0.70 $|e|$, +0.70 $|e|$, -0.49 $|e|$) around one vacancy and moments of the oppo-

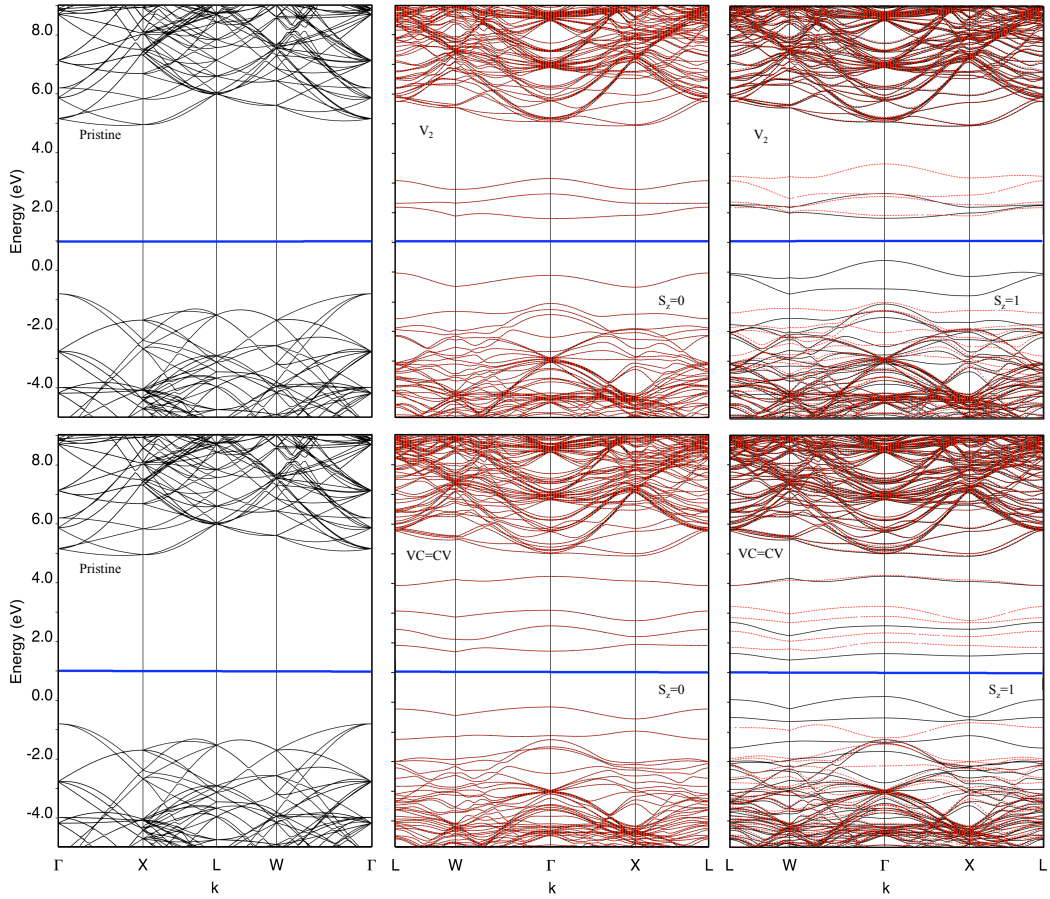


FIG. 3: B3LYP band structures of pristine diamond (1st panel), and the divacancies, V_2 (2nd panel) and $VC=CV$ (3rd panel), based on S_{128} calculations. For the latter two, singlet states are on the left and triplet on the right. Continuous black and dashed red lines indicate α and β bands, respectively. The horizontal blue line represents the Fermi energy.

site sign around the other. Additional points of interest with regard to V_2 are (i) that the degree of spin polarisation increases both with S_z and the percentage of exact exchange in the B3LYP functional, the UHF moments being close to unity; and (ii) that the PBE and LDA moments are extremely small, with a vanishing alternation of the α β spins in the singlet state. Mulliken population analysis, though undoubtedly useful, leads to an arbitrary partition of the electron distribution. A wider, more informative and unbiased description is contained in the charge and spin density maps. Figure 2 shows the singlet and triplet spin densities in planes containing V_2 and $VC=CV$ divacancies and nearest neighbours in a $\langle 111 \rangle$ chain from S_{128} calculations. The maps shown in this Figure provide direct graphical evidence as to reasons why the $\{\alpha\alpha\beta\}:\{\alpha\beta\beta\}$ singlet and $\{\alpha\alpha\beta\}:\{\alpha\alpha\beta\}$ triplet states (and the reverse spin alignments) are separated by only 2-3 meV, whereas the septet state is 60-80 meV higher in energy.

Turning now to band structures, Figure 3 shows these for pristine diamond, and the singlet and triplet states

of V_2 and $VC=CV$. The most striking, though not unexpected, feature of the divacancy band structures is the reduction in band gap from 5.76 eV to less than 2 eV in all cases. In the singlet states (central panels) the six unpaired/unbound electrons might be expected to occupy three pairs of bands (each α - β pair will result overlapped in the Figure) below the Fermi level, but above the valence bands, and three corresponding unfilled pairs of bands above the Fermi level, E_F , but below the conducting bands. However, for the V_2 divacancy, only 2 α - β pairs are well separated from those of the host lattice, leading to a band gap of 1.91 eV at the Γ -point. In the case of the higher energy $VC=CV$ divacancy, again there are only two pairs of occupied bands that are well separated from the valence bands, but now four empty pairs of bands between E_F and the host conduction bands appear, the fourth being the antibonding level of the double bond between the two vacancies. Here there is a band gap of 1.88 eV at the Γ -point. α and β bands, that are fully degenerate in $S_z=0$, split in $S_z=1$ (formally, 4α and 2β) as shown in Figure 3 (right panels), where the split-

ting is more evident in $VC=CV$ than in V_2 . For the latter the gap reduces to 1.0 for α electrons, whereas for β electrons it is much larger (2.6 eV). For $VC=CV$, numbers are similar, namely 1.1 and 2.2 eV for α and β electrons, respectively.

B. Vibrational properties

Vibrational spectroscopy makes a significant contribution to the identification of the different types of defects present in diamond. While it is generally rather difficult from experiment to assign a given spectral feature unambiguously to a specific structural defect, since, potentially, there are a large number of factors such as defect type, concentration, aggregation etc., that might hinder or complicate this. However, the same is not true for a simulation, since the nature of a particular defect, its concentration and local environment *i.e.*, bulk, surface grain boundary, presence of impurity etc., are defined precisely *a priori*.

The simulated Raman spectra of the singlet spin states of the V_2 and $VC=CV$ divacancy defects in diamond, derived from equilibrium B3LYP lattice structures and energy derivatives at concentrations corresponding to S_{64} and S_{128} supercells, are shown in Figure 4. The first panel contains the spectrum of the pristine host lattice, for comparison, the second and third, those for V_2 and the fourth and fifth, those for $VC=CV$. The full spectra have been obtained by enveloping each calculated frequency with a pseudo-Voigt function which consists of a linear combination of a Lorentzian and Gaussian functions with full width at half maximum of 8 cm^{-1} . The vertical blue line across the five panels marks the position of the simulated first-order Raman peak of pristine diamond obtained under the same computational conditions as the defective systems: it occurs at 1317 cm^{-1} , 15 cm^{-1} below the experimental peak.

The peak at 1317 cm^{-1} separates the spectra of the defective systems into two regions: at lower wavenumbers there are spectroscopic features due to collective vibrational modes with null intensity in perfect diamond for symmetry reasons. In the defective systems, these features have low relative intensity, and a comparison of the S_{64} and S_{128} spectra indicates that neither divacancy gives rise to specific features in this region of the spectrum. It is a reasonable assumption that peaks above 1317 cm^{-1} in the spectra of defective material that cannot be attributable to any vibrational modes, either inactive for symmetry reasons or with zero intensity, in the spectrum of pristine diamond, are due to defects. The experimental Raman spectrum of defective diamond, reported by Praver *et al.*²³, shows two major peaks in this region, at 1491 and 1628 cm^{-1} , the origins of which remain a matter of debate. Of various putative attributions, the most widely accepted for the 1628 cm^{-1} is the presence of sp^2 carbon atoms neighbouring the defect. Neither previous calculations for the isolated neutral va-

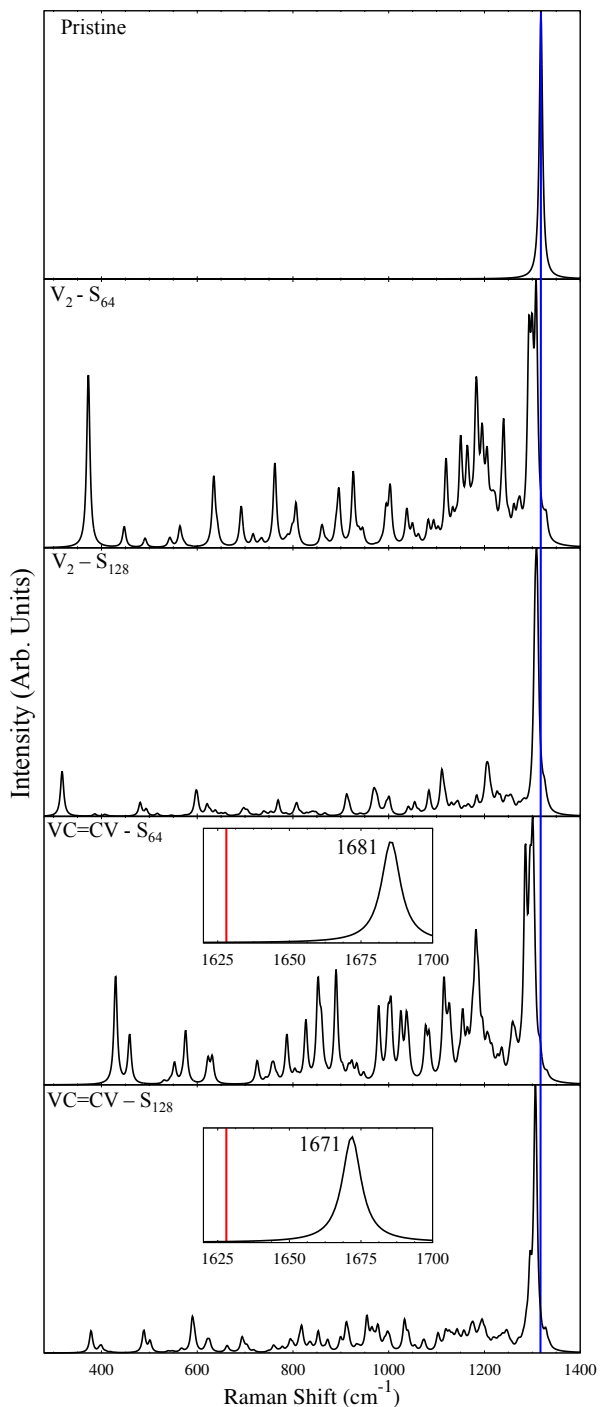


FIG. 4: B3LYP Raman spectra of S_{64} and S_{126} for pristine, V_2 and $VC=CV$ defective structures, the latter two in their most stable singlet spin state. The V_2 spectrum does not show any peak above 1317 cm^{-1} , whereas $V-C=C-V$ presents one peak. The spectral region between 1620 and 1700 cm^{-1} is also reported for this defect in the two boxes, where the vertical red line marks the position of the experimental²³ Raman signal at 1628 cm^{-1} .

cancy in diamond⁴³, nor the spectrum of the vicinal divacancy shown in Figure 4 exhibit a peak in this region, so that they can be excluded as potential candidates for the two peaks in the experimental spectrum. However, as the fourth and fifth panels of Figure 4 show quite clearly, single peaks occur at 1671 cm^{-1} and 1682 cm^{-1} respectively in the S_{64} and S_{128} spectra of the VC=CV divacancy. The limited dependence of the peak position on defect concentration reported here – the type of information which is notably absent in experimental spectra – suggests that even at lower concentrations the position of this peak is in the range $(1650\text{--}1660)\text{ cm}^{-1}$. Animations of the vibrational modes of the VC=CV divacancy (available at <http://www.pmpm.jussieu.fr/yves/defectsindiamond>) yield the contributions of the individual carbon atoms to the collective motion in the defective crystal, and show, specifically, that the $1671\text{ cm}^{-1}/1682\text{ cm}^{-1}$ peaks can be attributed to the C=C double bond. It is of interest to note that these values are close the range $1620\text{--}1680\text{ cm}^{-1}$ that have been reported for (molecular) alkenes.⁵⁹ Despite the reduction in intensity of this vibrational mode with decreasing concentration, as is the case with other modes, it remains approximately one quarter that of the first order Raman peak. Finally, the complete absence of intensity in the region of 1491 cm^{-1} in the spectra of both V_2 and VC=CV suggests that this feature of the spectrum reported by Praver *et al.*²³ is not attributable to either of these divacancies.

IV. CONCLUSIONS

The overall conclusion of this paper is that all-electron B3LYP hybrid calculations within a periodic supercell formulation provide a flexible and reliable approach to the structure, energetics, electronic and spin distributions and vibrational properties of lattice defects in crystalline solids. Specifically, in the case of vacancy defects in diamond the principal conclusions are:

- that the lowest energy states of the isolated neutral vacancy, V_1 , and both the vicinal V_2 and VC=CV divacancies, are singlets ($S_z=0$), followed by the

triplet ($S_z=1$) states;

- that the spin *alignment* in the singlet states of both divacancies is $\{\alpha\alpha\beta\}:\{\alpha\beta\beta\}$;
- that V_2 divacancies are more stable than VC=CV for all possible spin configurations, with a difference in energy of $\sim 1.7\text{ eV}$ for the singlet states;
- that the association, or binding energy of two (isolated) $S_z=0$ vacancies to form a singlet V_2 is $\sim 3.5\text{ eV}$;
- that the formation energies of 9.9 eV , 11.7 eV and 13.5 eV for V_2 , VC=CV and $2\times V_1$ respectively suggest that their native concentrations in diamond will be extremely small, and that their detectable presence is the result of (external) damage;
- that calculated defect energies from S_{64} and S_{128} supercells are effectively indistinguishable;
- that the use of richer basis sets than Pople's 6-21G leads to no meaningful differences in energy;
- that other hybrid functionals and one-electron approximations predict an identical pattern of stability with regard to V_2 and VC=CV;
- that the calculated first-order Raman peak in pristine diamond, 1317 cm^{-1} , is within 1% of the measured value, which gives weight to the description of the defective systems;
- that there is a small shift of $10\text{--}13\text{ cm}^{-1}$ of the first-order peak in the defective systems, which suggests that the perturbation of the lattice beyond the immediate vicinity of the divacancies is minimal;
- that neither divacancy gives rise to specific spectral features below the first-order peak;
- that the peak at $1671/1681\text{ cm}^{-1}$ in the spectrum of the VC=CV defective system, which is associated with the C=C double bond, is a candidate for the 1628 cm^{-1} peak reported by Praver *et al.*²³

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